# Atmospheric dynamics I

Clouds on the terrestrial planets



In one-dimensional model, the atmosphere is assumed to be horizontally uniform; however, this is not a good assumption in general.



3-D atmospheric circulation can play crucial roles in material transport



# Momentum equation

#### Pressure gradient force:



The x component of the pressure gradient force acting on a fluid element. Holton, 2004

#### Momentum equation in the inertial coordinate system

$$\frac{d\vec{v}}{dt} = -\frac{1}{\rho}\nabla p + \vec{g}$$

 $\vec{v}$  : velocity t : time  $\rho$  : atmospheric density p : atmospheric pressure  $\vec{g}$  : gravity acceleration



## Momentum equation in a rotating frame



### Momentum equation in a rotating frame

Let us consider a frame rotating at an angular velocity  $\vec{\Omega}$ .

For a position vector  $\vec{r}$ , the relationship between the time derivative in the inertial frame  $d_r/dt$  and that in a rotating frame d/dt is

$$\frac{d\vec{r}}{dt} = \frac{d_r\vec{r}}{dt} + \vec{\Omega} \times \vec{r}$$
  
$$\therefore \vec{v} = \vec{v}_r + \vec{\Omega} \times \vec{r} \qquad \vec{v}_r : \text{velocity in rotating frame}$$

Similarly

$$\frac{d\vec{v}}{dt} = \frac{d_r \vec{v}}{dt} + \vec{\Omega} \times \vec{v}$$

Combining these, using  $\vec{\Omega} \times (\vec{\Omega} \times \vec{r}) = -\Omega^2 \vec{R}$  we have

$$\frac{d\vec{v}}{dt} = \frac{d_r \vec{v}_r}{dt} + 2\vec{\Omega} \times \vec{v}_r - \Omega^2 \vec{R}$$

 $\vec{R}$  : vector from the rotational axis to the fluid position



Substituting the relationship into the momentum equation, one gets

$$\frac{d_r \vec{v}_r}{dt} = -2\vec{\Omega} \times \vec{v}_r - \frac{1}{\rho}\nabla p + \vec{g} + \Omega^2 \vec{R}$$

Hereafter the subscript r is omitted. The effective gravity acceleration is defined as the sum of  $\vec{g}$  and  $\Omega^2 \vec{R}$ . Then the momentum equation in the rotating frame is

$$\frac{\partial \vec{v}}{\partial t} = -\vec{v} \cdot \nabla \vec{v} - 2\vec{\Omega} \times \vec{v} - \frac{1}{\rho} \nabla p + \vec{g}$$

Next we consider an expression in a Cartesian coordinate system on a spherical surface. Using the velocity component (u, v, w) in the unit vector system  $(\vec{i}, \vec{j}, \vec{k})$ ,

 $\vec{v} = \vec{i} u + \vec{j} v + \vec{k} w$   $\vec{i}$ : eastward,  $\vec{j}$ : northward,  $\vec{k}$ : upward Then

$$\frac{d\vec{v}}{dt} = \vec{i}\frac{du}{dt} + \vec{j}\frac{dv}{dt} + \vec{k}\frac{dw}{dt} + u\frac{d\vec{i}}{dt} + v\frac{d\vec{j}}{dt} + w\frac{d\vec{k}}{dt}$$



**Figure 11.2** Spherical coordinates: longitude  $\lambda$ , latitude  $\phi$ , and radial distance *r*. Coordinate vectors  $e_{\lambda} = i$ ,  $e_{\phi} = j$ , and  $e_r = k$  change with position (e.g., relative to fixed coordinate vectors  $e_1$ ,  $e_2$ , and  $e_3$  of rectangular Cartesian coordinates).

Momentum equations (a: planetary radius)

$$\frac{du}{dt} = \left(2\Omega\sin\phi + \frac{u\tan\phi}{a}\right)v - \frac{uw}{a} - 2\Omega w\cos\phi - \frac{1}{\rho}\frac{\partial p}{\partial x}$$
$$\frac{dv}{dt} = -\left(2\Omega\sin\phi + \frac{u\tan\phi}{a}\right)u - \frac{vw}{a} - \frac{1}{\rho}\frac{\partial p}{\partial y}$$
$$\frac{dw}{dt} = \frac{u^2 + v^2}{a} - 2\Omega u\cos\phi - \frac{1}{\rho}\frac{\partial p}{\partial z} - g \qquad \qquad f = 2\Omega\sin\phi : \text{Coriolis parameter}$$

The shaded terms are "metric" terms arising from the spherical geometry. These are small on the Earth. (Venus is exception)

When dw/dt = 0, the equation in the vertical direction reduces to the hydrostatic equilibrium:

$$\frac{\partial p}{\partial z} = -\rho g$$



Figure 11.3 Planetary vorticity 2Ω decomposed into horizontal and vertical components

Neglecting the metric terms and defining  $\vec{v} = (u, v)$  as the horizontal component of the velocity, we have a set of governing equations:

$$\frac{\partial \vec{v}}{\partial t} = -\vec{v} \cdot \nabla \vec{v} - w \frac{\partial \vec{v}}{\partial z} - f\vec{k} \times \vec{v} - \frac{1}{\rho} \nabla p \qquad \text{horizontal momentum eq.} \\ \frac{\partial w}{\partial t} = -\vec{v} \cdot \nabla w - w \frac{\partial w}{\partial z} - \frac{1}{\rho} \frac{\partial p}{\partial z} - g \qquad \text{vertical momentum eq.} \\ \frac{\partial \rho}{\partial t} = -\nabla \cdot (\rho \vec{v}) \qquad \text{continuity eq.} \\ p = \rho RT \qquad \text{state eq.} \\ \frac{\partial \theta}{\partial t} = -\vec{v} \cdot \nabla \theta - w \frac{\partial \theta}{\partial z} + \frac{1}{c_p} \left(\frac{p_s}{p}\right)^{R/C_p} \dot{H} \qquad \text{thermodynamics eq.} \end{cases}$$

diabatic heating

$$\vec{k}$$
: unit vector in the vertical direction $f = 2\Omega \sin \phi$ : Coriolis parameter $\dot{H}$ : diabatic heating rate (J/m³/s)

## Pressure coordinate

Large-scale atmospheric motions satisfy hydrostatic equilibrium. In this case the pressure p can be used as the vertical coordinate:



300hPa, 2002/1/15



#### Primitive equations:

$$\frac{\partial \vec{v}}{\partial t} = -\vec{v} \cdot \nabla \vec{v} - \omega \frac{\partial \vec{v}}{\partial p} - f\vec{k} \times \vec{v} - \nabla \Phi \qquad \text{horizontal momentum eq.}$$

$$\frac{\partial \Phi}{\partial p} = -\frac{RT}{p} \qquad \text{state eq. + hydrostatic equilibrium}$$

$$\nabla \cdot \vec{v} + \frac{\partial \omega}{\partial p} = 0 \qquad \text{continuity eq.}$$

$$\frac{\partial \theta}{\partial t} = -\vec{v} \cdot \nabla \theta - \omega \frac{\partial \theta}{\partial p} + \frac{1}{c_p} \left(\frac{p_s}{p}\right)^{R/C_p} \dot{H} \qquad \text{thermodynamics eq.}$$

$$\vec{v} = (u, v) \qquad : \text{horizontal velocity}$$

$$\omega \qquad : \text{vertical velocity}$$

ω	. Vertical velocity
$\vec{k}$	: unit vector in the vertical direction
$f = 2\Omega \sin \phi$	: Coriolis parameter
H	: diabatic heating rate (J/m <sup>3</sup> /s)

## Geostrophic flow

For synoptic scale (>1000 km) motions in Earth's atmosphere: horizontal scale L ~ 1000 km pressure scale P ~ 1000 hPa velocity scale U ~ 10 m/s time scale L/U ~ 10<sup>5</sup> s Coriolis parameter f ~ 10<sup>-4</sup> Hz

$$\frac{\partial \vec{v}}{\partial t} = -\vec{v} \cdot \nabla \vec{v} - \omega \frac{\partial \vec{v}}{\partial p} - \frac{f\vec{k} \times \vec{v}}{Coriolis} - \frac{\nabla \Phi}{pressure}$$
force
$$\frac{10^{-4}}{10^{-4}} = 10^{-4} + 10^{-3$$

The ratio between the acceleration  $(U^2/L)$  and the Coriolis force (fU)

 $R_o = \frac{U}{fL}$  : Rossby number (around 0.1 on Earth, 10–100 on Venus)

Geostrophic flow becomes a good approximation for small Rossby numbers

Coriolis force  
$$f\bar{k} \times \vec{v}$$
  
H

Definition of geostrophic flow

 $f\bar{k} \times \vec{v}_g = -\nabla \Phi$ 

$$\vec{v}_g = \frac{1}{f}\vec{k} \times \nabla \Phi$$
 or  $u_g = -\frac{1}{f}\frac{\partial \Phi}{\partial y}, \quad v_g = \frac{1}{f}\frac{\partial \Phi}{\partial x}$ 

Geostrophic flow is two-dimensional:

$$\nabla \cdot \vec{v}_g = 0$$
$$\omega = 0$$

Geostrophic flow is not a good approximation near the equator (f is small) or for scales < O(100km) (L is small) where Ro (= U/fL) is large.

# Thermal wind

or

Differentiating  $f\bar{k} \times \vec{v}_g = -\nabla \Phi$  with respect to p and using  $\frac{\partial \Phi}{\partial p} = -\frac{RT}{p}$ , "thermal wind" relation is obtained:



Fig. 3.8 Relationship between vertical shear of the geostrophic wind and horizontal temperature gradients. (Note:  $\delta p < 0.$ )

#### Latitude-altitude cross section of Earth's atmosphere



#### Latitude-altitude cross section of Mars's atmosphere



(Smith et al. 2001)

# Geostrophic flow on Mars?

For synoptic scale (>1000 km) motions in Earth's atmosphere: horizontal scale L ~ 1000 km pressure scale P ~ 1000 hPa velocity scale U ~ 10 m/s on Earth  $\rightarrow$  100 m/s on Mars (westerly jet) time scale L/U ~ 10<sup>5</sup> s  $\rightarrow$  10<sup>4</sup> s on Mars Coriolis parameter f ~ 10<sup>-4</sup> Hz

$\frac{\partial \vec{v}}{\partial \vec{v}} =$	$-\vec{v}\cdot\nabla\vec{v}$ –					
0I <		dр	Coriolis force	pressure gradient force		
10 <sup>-4</sup>	10 <sup>-4</sup>	10 <sup>-4</sup>	10 <sup>-3</sup>	10 <sup>-3</sup>	(m s <sup>-2</sup> )	on Earth
10 <sup>-2</sup>	10 <sup>-2</sup>	10 <sup>-2</sup>	10 <sup>-2</sup>	10 <sup>-2</sup>	(m s <sup>-2</sup> )	on Mars

The ratio between the acceleration  $(U^2/L)$  and the Coriolis force (fU)

$$R_o \equiv \frac{U}{fL}$$
 : Rossby number (around 0.1 on Earth, 10–100 on Venus)  
around 1 on Mars ?

# Superrotation





Momentum equations



Atmospheric rotation takes the place of planetary rotation.

# Meridional force balance of zonal flow



## Thermal wind





 $\zeta = -\ln p$  : log-pressure altitude

#### Latitude-altitude cross section of Venus's atmosphere



Fig. 2. Meridional cross section of atmospheric temperature (K) obtained combining 116 VeRa profiles. Hemispherical symmetry and local time independence has been assumed. Contours have been smoothed. Contours interval is 10 K, some contours have been removed to render the plot clearer.

Westward wind



Fig. 8. Latitude-height cross section of zonal thermal wind speed (m s<sup>-1</sup>) derived from VeRa temperature profiles assuming cyclostrophic balance (Eq. (5)). The velocity used as lower boundary condition is the cloud-tracked wind profile retrieved from VIRTIS/VEx 1.74  $\mu$ m images (Sánchez-Lavega et al., 2008). Contour interval is 10 m s<sup>-1</sup>.

#### Latitude-altitude cross section of Venus's atmosphere

Cloud-tracked zonal winds around 70 km (Sánchez-Lavega et al. 2017)



Zonal winds determined from cyclostrophic balance (Piccialli et al., 2012)



**Fig. 8.** Latitude-height cross section of zonal thermal wind speed (m s<sup>-1</sup>) derived from VeRa temperature profiles assuming cyclostrophic balance (Eq. (5)). The velocity used as lower boundary condition is the cloud-tracked wind profile retrieved from VIRTIS/VEx 1.74  $\mu$ m images (Sánchez-Lavega et al., 2008). Contour interval is 10 m s<sup>-1</sup>.

The discrepancy is not understood

Radiative energy budget and meridional circulation



Fig. 10.7 Streamfunction (units: 10<sup>2</sup> kg m<sup>-1</sup>s<sup>-1</sup>) for the observed Eulerian mean meridional circulation for Northern Hemisphere winter, based on the data of Schubert et al. (1990).

Horizontal convection  $\rightarrow$  Hadley circulation



Fig. 3.11 Adjustment of surface pressure to midtropospheric heat source. Dashed lines indicate isobars.

Holton (1992)

Radiative energy budget and meridional circulation



Space and time-scales of dynamical atmospheric processes



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# Rotational wind and divergent wind

The horizontal velocity vector can be expressed with the stream function  $\,\psi\,$  and the velocity potential  $\phi\,$  :



Rotational component is nondivergent

 $\nabla \cdot (\vec{k} \times \nabla \psi) = 0$  : geostrophic flow, Rossby wave

Divergent component is irrotational

 $\nabla \times \nabla \phi = 0$  : convection, gravity wave

# Planetary-scale motions



(divergent flow) Hadley circulation Subsolar-to-antisolar circulation









# Atmospheric waves

- generated in an unstable background atmosphere
- can transport momentum and energy over long distances
- can induce mixing of the atmosphere

ightarrow Waves play crucial roles in the development of planetary-scale atmospheric structure





# Atmospheric waves

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Rossby wave (horizontal oscillation)

Gravity wave (vertical oscillation)



Salby (1996)

# Vorticity

The *circulation C* about a closed contour is defined as the line integral along the contour of the component of the velocity vector that is locally tangent to the contour:

$$C = \oint_{l} \vec{v} \cdot d\vec{l} = \oint_{l} |\vec{v}| \cos \alpha dl = \iint_{S} (\nabla \times \vec{v}) \cdot \vec{n} dS$$

n : unit vector normal to the surface

(Stokes' theorem was used.)

Dividing the circulation  $\delta C$  encircling a small area  $\delta S$ , and considering the limit  $\delta S \rightarrow 0$ , we get the *vorticity*:

$$\zeta = \frac{\delta C}{\delta S} = (\nabla \times \overline{v}) \cdot \overline{k}$$
$$= \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y}$$



# Quasi-geostrophic approximation



The real wind is divided into geostrophic wind and ageostrophic wind.

$$\vec{v} = \vec{v}_g + \vec{v}_a \qquad \qquad \frac{v_a}{v_g} = O(R_o) \ll 1$$
$$\vec{v}_g = \frac{1}{f_0} \vec{k} \times \nabla \Phi \qquad \qquad \qquad R_o = \frac{U}{fL}$$

The ratio of the magnitudes of the ageostrophic and geostrophic winds is the same order of magnitude as the Rossby number (around 0.1 in Earth's atmosphere)

Lagrangian derivative:

$$\frac{d}{dt} = \frac{\partial}{\partial t} + \vec{v} \cdot \nabla + \omega \frac{\partial}{\partial p}$$

The advection term is approximated by advection by geostrophic wind:

$$\frac{d_g}{dt} \equiv \frac{\partial}{\partial t} + \vec{v}_g \cdot \nabla$$

# Beta-plane approximation

The first-order Taylor series approximation of the Coriolis parameter *f* :

$$f = 2\Omega \sin \phi$$
  

$$\sim 2\Omega [\sin \phi_0 + (\phi - \phi_0) \cos \phi_0]$$
  

$$= f_0 + \beta y$$

where

$$f_0 = 2\Omega \sin \phi_0$$
$$\beta = \frac{2\Omega}{a} \cos \phi_0 \sim \frac{df}{dy}$$

Mid-latitude beta-plane :  $f = f_0 + \beta y$ Equatorial beta-plane :  $f = \beta y$ 



# Quasi-geostrophic vorticity equation

Introducing beta-plane approximation to the quasi-geostrophic Lagrangian derivative and retaining small quantities to the first order, the rate of change of the geostrophic wind is given by

$$\left(\frac{\partial}{\partial t} + \vec{v}_g \cdot \nabla\right) \vec{v}_g = -(f_0 + \beta y) \vec{k} \times (\vec{v}_g + \vec{v}_a) - \nabla \Phi$$
$$\sim -f_0 \vec{k} \times \vec{v}_a - \beta y \vec{k} \times \vec{v}_g \tag{1}$$

 $(\vec{v}_g = \frac{1}{f_0}\vec{k} \times \nabla\Phi \text{ was used})$ 

Since geostrophic wind is nondivergent (  $\nabla \cdot \vec{v}_{g}$  = 0 ), the continuity eq. is

$$\nabla \cdot \vec{v}_a + \frac{\partial \omega}{\partial p} = 0 \tag{2}$$

Operating rotation ( $\nabla \times$ ) to (1) and using (2), we have the quasi-geostrophic vorticity equation.

Quasi-geostrophic vorticity equation:

$$\frac{\partial \zeta_g}{\partial t} = -\vec{v}_g \cdot \nabla(\zeta_g + f) + f_0 \frac{\partial \omega}{\partial p}$$
$$\zeta_g = \frac{\partial v_g}{\partial x} - \frac{\partial u_g}{\partial y} = \frac{\nabla^2 \Phi'}{f_0} \quad : \text{geostrophic vorticity}$$

Vorticity changes with time through

- advection of absolute vorticity ( $\varsigma_g + f$ ) by geostrophic wind ( $\vec{v}_g$ )
- vertical divergence (horizontal divergence)



Fig. 4.7 A cylindrical column of air moving adiabatically, conserving potential vorticity.

# Rossby wave

Let us consider a two-dimensional motion ( $\omega$  = 0)

$$\left(\frac{\partial}{\partial t} + \vec{v}_g \cdot \nabla\right) (\xi_g + f) = 0$$

→ Absolute vorticity ( $\varsigma_g + f$ ) is conserved along the geostrophic wind  $\vec{v}_g$ .

A basic state where a homogeneous zonal flow exists:



The deviation from the basic state is denoted by ()' :

$$\frac{\partial}{\partial t}\zeta_{g} + (\overline{u} + u_{g}')\frac{\partial\zeta_{g}}{\partial x} + v_{g}'\frac{\partial\zeta_{g}}{\partial y} + v_{g}'\beta = 0$$
(1)

The velocity and vorticity are related to the geopotential perturbation

$$\xi'_{g} = \frac{\nabla^{2} \Phi'}{f_{0}}, \ u'_{g} = -\frac{1}{f_{0}} \frac{\partial \Phi'}{\partial y}, \ v'_{g} = \frac{1}{f_{0}} \frac{\partial \Phi'}{\partial x}$$

Substituting these into (1) and retaining first order terms only, we get

$$\frac{\partial}{\partial t}\nabla^2 \Phi' + \overline{u}\frac{\partial}{\partial x}\nabla^2 \Phi' + \beta \frac{\partial \Phi'}{\partial x} = 0$$

Assuming a wave solution  $\Phi' = \hat{\Phi} \exp[i(kx + ly - kct)]$ , the phase velocity of Rossby wave is obtained as:

$$c-\overline{u}=-\frac{\beta}{k^2+l^2}$$

k: zonal wavenumberl: meridional wavenumberc: zonal phase velocity

- Propagation opposite to the planetary rotation
- β effect (latitude variation of the Coriolis parameter *f*) is needed.
- Longer waves (smaller k) propagate faster.

The wave possesses angular momentum in the direction opposite to the planetary rotation





## Propagation of Rossby waves





Figure 14.16 Schematic illustrating the reaction of an air parcel to meridional displacement. Displaced equatorward, an eastward-moving parcel spins up cyclonically to conserve absolute vorticity. Northward motion induced ahead of it then deflects the parcel's trajectory poleward back toward its undisturbed latitude. The reverse process occurs when the parcel overshoots and is displaced poleward of its undisturbed latitude.

Salby (1996)

Rossby waves in planetary atmospheres



Earth



Saturn



Mars (MGS/TES temperature)

### Rossby waves on Venus







Linear solution of Rossby wave at 70 km (Kouyama et al. 2015)

The superrotation of the atmosphere takes the place of planetary rotation.

# Gravity wave

In Cartesian coordinates, without the assumption of hydrostatic equilibrium, the governing equations are:

$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + w \frac{\partial u}{\partial z} = \frac{1}{\rho} \frac{\partial p}{\partial x}$$
$$\frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + w \frac{\partial w}{\partial z} = -\frac{1}{\rho} \frac{\partial p}{\partial z}$$
$$\frac{\partial \rho}{\partial t} = -\frac{\partial(\rho u)}{\partial x} - \frac{\partial(\rho w)}{\partial z}$$
$$\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + w \frac{\partial \theta}{\partial z} = 0$$
$$\theta = \frac{p}{\rho R} \left(\frac{p_s}{p}\right)^{R/C_p}$$
T

horizontal momentum eq. (x-axis only)

vertical momentum eq.

continuity eq.

thermodynamics eq.

Equations for disturbances:

$$\overline{\rho} \frac{\partial u'}{\partial t} = -\frac{\partial p'}{\partial x}$$

$$\overline{\rho} \frac{\partial w'}{\partial t} = -\frac{\partial p'}{\partial z} - \rho' g$$

$$\frac{\partial \rho'}{\partial t} = -\overline{\rho} \frac{\partial u'}{\partial x} - \frac{\partial (\overline{\rho} w')}{\partial z}$$

$$\frac{1}{\overline{\theta}} \frac{\partial \theta'}{\partial t} + w' \frac{N^2}{g} = 0$$

$$\rho' = \frac{p'}{c_s^2} - \overline{\rho} \frac{\theta'}{\overline{\theta}}$$

horizontal momentum eq. (x-axis only)

vertical momentum eq.

continuity eq.

thermodynamics eq.

$$c_s^2 = \frac{c_p}{c_v} RT$$
 c<sub>s</sub>: sound speed  
 $N^2 = g \frac{d \ln \overline{\theta}}{dz}$  N: buoyancy frequency

Assuming an isothermal atmosphere:

$$N^{2} = g/c_{p}T$$
$$\overline{\rho}(z) = \rho_{s} \exp(-z/H)$$

Substituting the wave solution  $w'(x,z,t) = \hat{w}(z)\exp[i(kx + \sigma t)]$ ( $\sigma$ : frequency) into the governing equations before, an equation for the vertical velocity w is obtained as

$$\frac{d^2(\overline{\rho}\hat{w})}{dz^2} + \frac{1}{H}\frac{d(\overline{\rho}\hat{w})}{dz} + \left[\frac{\sigma^2}{c_s^2} - k^2 + \frac{N^2k^2}{\sigma^2}\right]\overline{\rho}\hat{w} = 0$$

Considering the amplitude growth with height in a stratified atmosphere, w is assumed to have the form

$$\hat{w}(z) = W(z) \exp(z/2H) \iff \overline{\rho} \hat{w}^2(z) \propto W^2(z)$$

Then the equation becomes

$$\frac{d^2W}{dz^2} + \left[\frac{\sigma^2}{c_s^2} - k^2 + \frac{N^2k^2}{\sigma^2} - \frac{1}{4H^2}\right]W = 0$$

Assuming a wave solution  $W \propto \exp(imz)$  (*m*: vertical wavenumber), the dispersion relation is obtained:

$$m^{2} = \frac{\sigma^{2}}{c_{s}^{2}} - k^{2} + \frac{N^{2}k^{2}}{\sigma^{2}} - \frac{1}{4H^{2}}$$

Solutions for acoustic-gravity wave and internal gravity wave exist.

Approximate solution for internal gravity wave is

$$\sigma^2 = \frac{N^2 k^2}{k^2 + m^2 + \frac{1}{4H^2}} \qquad \Rightarrow \sigma < N$$

#### Structure of gravity wave

For large-horizontal scale waves (typical in planetary atmospheres),



Fig. 7.9 Idealized cross section showing phases of pressure, temperature, and velocity perturbations for an internal gravity wave. Thin arrows indicate the perturbation velocity field, blunt solid arrows the phase velocity. Shading shows regions of upward motion.





Amplitude growth with height and wave breaking
→ turbulence generation, mean-wind acceleration

## Observed gravity waves



Mountain waves on Earth



Mountain waves on Mars



Fig. 11. VMC images of polar waves: left - long waves (NIR1 filter), middle - long waves producing short wave trains (UV), right - imegular waves (UV).

on Venus



Topographically-generated gravity waves (mountain waves) on Venus





Mountain wave discovered on Venus

# Thermal tides

Planetary-scale gravity wave generated by the movement of the solar heating region in the diurnal cycle



Excitation mechanism:

- Earth : solar heating of stratospheric ozone layer
- Venus : solar heating of cloud layer
- Mars : solar heating of atmospheric dust

## Thermal tide in Earth's atmosphere



Fig. 4.7. (a) Amplitude and (b) phase of solar diurnal component of T at various latitudes for equinox. [After Lindzen (1967).]

Holton (1992)

# Thermal tide in Venus's atmosphere



Temperature perturbation (Schofield & Taylor 1983)



# Wind field of thermal tides on Venus observed by Akatsuki infrared camera (Fukuya et al. 2021)

#### Clouds seen in thermal IR







- Equatorward circulation was discovered on the nightside
- Dayside poleward flow and the nightside equatorward flow cancel each other